

# LABOR-CAPITAL RELATIONS IN THE CONSTRUCTION SECTOR IN POLAND

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**Abstract.** The aim of this paper is to estimate the Cobb-Douglas production function and the CES (constant elasticity of substitution) function for the construction sector in Poland. The period since 2002 is analyzed. Moreover, the Solow decomposition of the economic growth is estimated. Most of the models are linearized in order to apply the ordinary least squares for linear regression models. The CES function is estimated both with a help of Kmenta approximation and the nonlinear least squares (NLS) using a variant of the Levenberg–Marquardt algorithm. In a short literature review some recent findings for Polish economy are briefly reminded in the context of the current research. Finally, it is concluded that the technological progress (both in the national economy and in the construction sector) is approximately 3%. The Cobb-Douglas function is preferred over the CES function, both in the national economy and in the construction sector. Elasticities of the labor are greater than elasticities of the capital.

**Key words:** capital, Cobb-Douglas function, employment, structural changes, total factor productivity.

## 1. Introduction

Poland is an example of the post-communist economy, which transited into a well-working capitalist system. Although, in 1990s – due to transition processes, privatization and closing of unprofitable factories – high unemployment emerged in certain regions of the country (see, for example, Newell, 2006), afterwards the economy developed in a very dynamic way.

Poland accessed the European Union in 2004. Except a high dynamic of the economic development, many (especially

young and qualified) people emigrated to more developed countries of the so-called “old” EU countries.

However, Polish cities noticed many new investments. Highways were build linking various cities, roads were repaired and the mobility of the labor force increased very much. Not only the physical development played its significant role, but also social and cultural changes were important.

In 2000s many significant changes in the education system were made, resulting in

a great demand for the university education amongst young people. Also, cities itself become sources of new workplaces and opportunities to make a career and find a well-paid job.

The average prices on the housing market increased between 2006 and 2013 by almost 26%. However, in the same period these prices increased by more than 65% in 10 biggest cities of Poland. In the most dynamically developing cities the prices increased even by 80% - just between 2005 and 2006. For a review see, for example, Augustyniak et al. (2012), Drachal (2014), Drachal (2013) and references therein.

Such changes must have had some impact on GDP (gross domestic product) and productivity (Bratsberg and Raaum, 2012; Zheng, Chau and Hui, 2012). However, it seems that the classical analysis with a help of Cobb-Douglas function has not been done yet. Actually, there is a work of Tomaszewicz and Świerczewska (2008) covering various sectors of economy, but it contains the sample from the period between 1993 and 2005 only. There is also the analysis by Tokarski (2007), in which it is stated that regions of Poland with a high ratio of value added in construction have also a lower level of TFP (total factor productivity). Tokarski's analysis is based on a sample between 1995 and 2007. Some partial analysis of the construction sector for Poland was also done by Kalinowski (2002).

The aim of this paper is to estimate the Cobb-Douglas and the CES (constant elasticity of substitution) functions for Poland, both in general (to have a comparison) and for the construction sector only. Moreover, the Solow decomposition is estimated and

discussed. The period after 2002 is analyzed.

## 2. Literature review

The Cobb-Douglas production function is a well-known tool in the economic analysis. It is usually used to estimate the potential GDP and TFP. For some interesting modifications see, for example, the discussion by Jerzmanowski (2007). An interesting discussion is also presented, for example, by Growiec (2008), Welfe (2011) and Welfe (2013).

Unfortunately, in the case of Poland the Cobb-Douglas function approach is able to explain only 10-30% of the potential GDP increase between 1966 and 1998 (Welfe, 2002).

The review of TFP for various developing countries was presented by Saliola and Seker (2011). Denis, McMorrow and Roeger (2002) analyzed EU countries before 2002. The manufacturing sector of EU countries was analyzed by Fioramanti (2010). Some interesting discussion in the context of the East European transition economies was presented by Funke and Ruhwedel (2005). The recent overview of GDP structure of various EU countries was presented, for example, by Vinerean (2013).

However, for example, Hlousek (2007) argued that aspects such as preferences, technology and government policies should be viewed as fundamentals - especially in case of Visegrad states. Also, Hall and Jones (1999) discussed differences in capital accumulation, productivity and output per worker. They found that these factors are driven mainly by differences in institutions and government policies, i.e., the social infrastructure. Such an infrastructure is determined by the historical location and

similar factors. As a result, they argued that the Cobb-Douglas approach can be biased.

Indeed, there is also another significant problem. Estimations based on samples containing periods before the transition in Poland suffer from comparability with capitalist economies. If various production functions are considered, then, usually the Cobb-Douglas estimations are found superior over the CES (see, for example, Epstein and Macchiarelli, 2009; Hacker, Johansson and Karlsson, 2004; Kemme, 1984; Roberts, 1994; Bairam, 1987).

In case of Poland, after the EU accession the transfer of technologies is found as a very important factor driving the productivity growth (Kolasa, 2005). Gawrycka, Sobiechowska-Ziegiert and Szymczak (2012) found that the increase in the production between 1991 and 2008 in Poland was mainly the result of the capital growth. However, for the period between 1998 and 2008 it was the technological progress. Similar results, emphasizing the role of the technological progress in Poland, were found by Benkovskis et al. (2013).

Caselli and Tenreyro (2005) discussed four types of a convergence. One of these types is a structural transformation being the result of a reallocation of production factors between different sectors of the economy. Such changes are usually dynamical in periods of accelerated technological and organizational progress. Therefore, it is interesting to analyze the period after EU accession for Poland.

Moreover, Kosztowniak (2013) stated that Foreign Direct Investments played a significant role in economic development

in Poland after the transition. Its main influence was by the transfer of new technologies. Kosztowniak (2013) analyzed the period between 1995 and 2012. Some modification of the classical Cobb-Douglas function was used in this research. Gurgul and Lach (2012) analyzed the impact of a technological progress on the economic growth in Poland in 2000s (2012).

Roszkowska (2013) discussed various aspects of the relationship between the human capital and economic growth for Poland in a current perspective. Jabłoński (2005) analyzed the period between 1990 and 2001. It was found in their researches that the most significant factor of the economic growth is the human capital. Indeed, Welfe (2008) presented arguments why “new economies” are mostly based on knowledge and how it implies the significant role of human capital in the context of TFP analysis. General discussion on human capital in the context of growth models is given by, for example, Zhang (2014).

Finally, it should be mentioned that there are some arguments that relative (i.e., construction sector to total economy) TFP can drive house prices. A significant negative contribution of a relative TFP to construction prices was found in the U.K. and Spain. On the other hand, in the United States and Germany this contribution was found positive (Moro and Nuno, 2010). The analyzed sample consisted of the period between 1980 and 2007.

Applicability of various growth models was recently discussed, for example, by Durlauf, Kourtellos and Tan (2008), Leon-Ledesma, McAdam and Willman (2013) and Herrendorf and Valentinyi (2012). Of

course, also papers by Mankiw, Romer and Weil (1992) and Fisher (1993) are very important. Definitely, such models are significant for the analysis of the construction sector (Herrendorf, Herrington and Valentinyi, 2013; Nasir et al., 2014; Dolage and Chan, 2013; Ruddock and Ruddock, 2011).

### 3. Methodology

The Cobb-Douglas production function (Cobb and Douglas, 1928) is a well-known tool in economic analysis (Felipe and Adams, 2005). It is also simple to estimate. However, one should be careful in economic interpretations, because Miller (2008) and Aiyar and Dalgaard (2009) presented a critique that this simplicity can lead to well-looking numerical outcomes, which do not provide interpretations satisfactory from the economic interpretation. Some doubts are also presented by Antras (2004) in case of the United States economy.

Further, the following notation of variables used in the econometric analysis is used.  $K$  denotes the gross value of fixed assets in thousands of PLN in 2002 prices.  $L$  denotes the number of employed persons in the national economy in thousands.  $GDP$  is given in millions of PLN in 2002 prices. The symbol “ $\ln$ ” before a variable means that it is the natural logarithm of the original variable. The symbol “ $\ln^2$ ” before a variable means that this variable has been squared. The variables corresponding to the construction sector are marked with the letter “ $c$ ”, in order to differentiate from the data from the whole national economy. The yearly dynamic of  $K$  is denoted by  $gK$  and the yearly dynamic of  $K_c$  is denoted by  $gK_c$ . Similar notation is used for variables  $L$  and  $L_c$ . The variable time has value 0 for 2002 year and it enumerates the following years, taking

value 11 for 2013 year. The variable  $KL$  denotes the ratio  $K/L$ . The symbol “ $\wedge$ ” stands for the exponentiation.

According to the above notation the Cobb-Douglas function can be expressed in the following way

$$(1) \quad GDP = \text{const} * K^a * L^b,$$

which can be transformed into the linear equation

$$(2) \quad \ln GDP = \ln \text{const} + a * \ln K + b * \ln L.$$

The last equation is linear and parameters  $\text{const}$ ,  $a$  and  $b$  can be estimated by the ordinary least squares method.

The linear regression analysis is not always applicable. It is assumed that there is no heteroskedasticity (i.e., the variance is constant), residuals are normally distributed and not autocorrelated. These assumptions can be tested, for example, by White's test, Jarque-Bera test and LM test, respectively. Moreover, the specification of the model can be tested by RESET test (Montgomery, Peck and Geoffrey Vining, 2012; Hill, Griffiths and Lim, 2011).

The Cobb-Douglas function is a special case of the CES function (Solow, 1956). For a review of various growth models see, for example, the book by Barro and Sala-i-Martin (2004). The CES function is given by the following equation

$$(3) \quad GDP = \gamma * [\delta * K^{(-\rho)} + (1 - \delta) * L^{(-\rho)}]^{(-\mu / \rho)},$$

which can be linearized in the following way

$$(4) \quad \ln GDP = \ln \gamma - (\mu / \rho) * \ln [\delta * K^{(-\rho)} + (1 - \delta) * L^{(-\rho)}].$$

Unfortunately, the last equation is still nonlinear and the ordinary least squares method cannot be applied. One of the possible solutions is to use the Kmenta approximation (Kmenta, 1967; Greene, 2003), i.e., to estimate the following linear equation

$$(5) \quad \ln_{GDP} = \ln_{\gamma} + \mu * \delta * \ln_K + \mu * (1 - \delta) * \ln_L - 0.5 * \rho * \mu * \delta * (1 - \delta) * \ln_{KL}.$$

If  $\rho$  is close to 0, then the error in Kmenta approximation is small.

However, parameters of nonlinear equations can also be estimated directly. One of the possible methods is to use the nonlinear least squares (NLS) and the Levenberg-Marquardt algorithm (see, for example, Henningsen and Henningsen, 2011). The estimation of the CES function is non trivial. Various discussions on this topic and the economic interpretation can be found, for example, in papers by Thursby (1980), Hodges (1969), Nelson (1965), Zarembka (1970), Klum, McAdam and Willman (2012), Koesler and Schymura (2012), Temple (2012) and Henningsen and Henningsen (2012).

In the Cobb-Douglas function, i.e.,

$$GDP = \text{const} * K^a * L^b,$$

the parameter  $\text{const}$  is not time dependent. It should be time dependent, if technological progress is assumed. Then, by differentiating (see, for example, Barro and Sala-i-Martin, 2004) the above equation with respect to time, the following equation is obtained

$$(6) \quad gGDP = g_c + a * gK + b * gL,$$

where  $g_c$  can be interpreted as the dynamic of the technological progress,

$gK$  – the dynamic of the capital growth,  $gL$  – the dynamic of the labor force growth and  $gGDP$  as GDP dynamics. Of course, this equation can be estimated by the ordinary least squares method. It is called the Solow decomposition (Arrow et al., 1961).

The discussion of the original Solow growth model can be found, for example, in papers by McQuinn and Whelan (2007), Gundlach (2005), Burda and Severgnini (2014), Carter (2011) and Neuhaus (2006).

Sometimes, the Cobb-Douglas function is also discussed in the following form

$$(7) \quad GDP = \text{const} * e^{(g * \text{time})} * K^a * L^b.$$

Then, the parameter  $g$  is interpreted as the technological progress in a sense of Hicks (i.e., the one not changing the marginal rate of substitution between capital and labor) and  $e$  denotes the base of the natural logarithm. This equation can be linearized in the following way

$$(8) \quad \ln_{GDP} = \ln_{\text{const}} + g * \text{time} + a * \ln_K + b * \ln_L$$

and estimated by the ordinary least squares method.

The yearly data from the period between 2002 and 2013 were obtained from Central Statistical Office of Poland (GUS, 2015). ESA 2010 (European Union, 2013) and PKD 2007 (Dz. U. z 2007 r. Nr 251, poz. 1885) methodologies are applied. The calculations were done in GRETL (2015).

#### 4. Results and their interpretation

If it is not stated otherwise, the 5% p-value is assumed.

Table 1 presents the estimation and the diagnostic of Eq. (2), which corresponds to the Cobb-Douglas function of the national economy given by Eq. (1). All estimated parameters are statistically significant. The R-squared is very high. Assumptions of a regression model are not violated. However, the null hypothesis of an adequacy of the specification of the model can be rejected. The sum of coefficients is greater than 1, which can be interpreted as increasing returns to scale. The elasticity of labor is greater than 1, whereas the elasticity of capital is smaller than 1.

Table 2 presents the estimation and the diagnostic of Eq. (2), which corresponds to the Cobb-Douglas function of the construction sector given by Eq. (1). In the first estimation the const coefficient was statistically not significant. Therefore, it was rejected from the model. The R-squared of the obtained model is very high. All assumptions of a regression model are not violated. Also, the adequacy of the specification of the model cannot be rejected. The sum of coefficients is slightly greater than 1, which can be interpreted as increasing returns to scale. However, these returns are smaller than the average for the national economy. Elasticities are smaller than 1. Both of them in the construction sector are smaller than the ones in the national economy.

Table 3 presents the estimation and the diagnostic of Eq. (8), which corresponds to the Cobb-Douglas function of the national economy given by Eq. (7). In the first estimation not all estimated parameters were statistically significant. As a result, only time and labor remained in the final model. The R-squared is very high. Assumptions of a regression model are not violated. However, the null

hypothesis of an adequacy of the specification of the model can be rejected. The sum of coefficients is greater than 1, which can be interpreted as increasing returns to scale. The elasticity of labor is greater than 1. The technical progress is estimated to be approximately 2%. Unfortunately, the lack of variable corresponding to the capital makes the obtained model questionable from the interpretation point of view.

Table 4 presents the estimation and the diagnostic of Eq. (8), which corresponds to the Cobb-Douglas function of the construction sector given by Eq. (7). In the first estimation the capital parameter was statistically not significant. The R-squared of the final model is very high. Assumptions of a regression model are not violated. Also, the hypothesis of an adequacy of the specification of the model cannot be rejected. The sum of coefficients is greater than 1, which can be interpreted as increasing returns to scale. The elasticity of labor is smaller than 1. It is also smaller than in the corresponding model of the national economy. The technical progress is estimated to be approximately 3%. Unfortunately, the lack of variable corresponding to the capital makes the obtained model questionable from the interpretation point of view, as in the previous case.

Table 5 presents the estimation and the diagnostic of the Solow decomposition, given by Eq. (6), for the national economy. In the first estimation the capital parameter was statistically not significant. The R-squared of the final model is small. Assumptions of a regression model are not violated. Also, the hypothesis of an adequacy of the specification of the model cannot be rejected. The sum of coefficients is

smaller than 1, which can be interpreted as decreasing returns to scale. The elasticity of labor is smaller than 1. The technical progress is estimated to be approximately 3%. Unfortunately, the lack of variable corresponding to the capital makes the obtained model questionable from the interpretation point of view.

Table 6 presents the estimation and the diagnostic of the Solow decomposition, given by Eq. (6), for the construction sector. In the first estimation the capital parameter and the constant were statistically not significant. The R-squared of the final model is moderately high. Assumptions of a regression model are not violated. Also, the hypothesis of an adequacy of the specification of the model cannot be rejected. The sum of coefficients is smaller than 1, which can be interpreted as decreasing returns to scale. The elasticity of labor is smaller than 1. It is smaller than in the corresponding model of the national economy. The technical progress is estimated to be approximately 3%. Unfortunately, the lack of variable corresponding to the capital makes the obtained model questionable from the interpretation point of view.

Table 7 presents the estimation and the diagnostic of the Kmenta approximation of the CES function of the national economy, given by Eq. (5). The estimated productivity is very small. Parameter rho is approximately -0.0015. The elasticity of substitution is approximately 1.0015. The parameter mu is approximately 1.76, which indicates increasing returns to scale. Therefore, the Cobb-Douglas function should be a good approximation of the CES function in this case. Unfortunately, the estimated parameter delta is greatly over 1, which means that

the obtained model is not good for the economic interpretation. For the explicit formulas, see, for example, Henningsen and Henningsen (2011). The R-squared of the estimated model is high. Assumptions of a regression model are not violated. Also, the hypothesis of an adequacy of the specification of the model cannot be rejected.

Table 8 presents the estimation and the diagnostic of the Kmenta approximation of the CES function of the construction sector, given by Eq. (5). Unfortunately, all parameters were statistically not significant in the first estimation. Rejection of the parameter with the highest p-value (i.e.,  $l_{Kc}$ ) resulted in a model with parameters statistically significant (10% p-value). The estimated productivity is very high, i.e., approximately 3.85. Parameter delta is assumed to be 0, which makes the parameter rho goes to infinity. As a result, the CES function turns to the Leontief function. In other words, there is no substitutability between labor and capital in the construction sector, according to the Kmenta approximation.

Table 9 presents the estimation of the CES function for the national economy by the nonlinear least squares (NLS) method. The CES function is given by Eq. (3). Table 9 presents the estimation of the modified equation, i.e. Eq. (4). The variable K1 is K divided by 1000. Similarly, the variable L1 denotes L divided by 1000. Such divisions were done due to certain numerical problems. The parameter mu is approximately 2.22, which indicates increasing returns to scale. The parameter rho is statistically not significant. In other words it can be assumed to be equal to 0. It means that the CES function reduces to the Cobb-Douglas function.

Table 10 presents the estimation of the CES function for the construction sector by the nonlinear least squares (NLS) method. The CES function is given by Eq. (3). Table 10 presents the estimation of the modified equation, i.e. Eq. (4). The parameter  $\mu$  is approximately 1.15, which indicates increasing returns to scale. The parameter  $\rho$  is statistically not significant. In other words it can be assumed to be equal to 0. It means that the CES function reduces to the Cobb-Douglas function.

### 5. Conclusions

Most of estimated models indicate increasing returns to scale, both for the national economy and the construction sector. However, returns in the construction sector are lower than in the national economy. On the other hand, the estimated technological progress has similar value in the national economy and in the construction sector, i.e., approximately 3%. The detailed values differ between 2.4% and 3.2% depending on the model used. Therefore, it can be concluded that the real value is some value from the between. In comparison to previous researches (cited in the first part of this paper) such values seem probable and reasonable. Elasticities of the labor are greater than elasticities of the capital. As a result, it can be argued that most of the growth is due to the labor, not due to the capital. In one case, even the Leontief function was found. Finally, it seems that the Cobb-Douglas function is the preferred specification over the CES function both in the construction sector and in the national economy.

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**Table 1.** Estimation and diagnostic of the OLS model. Dependent variable:  $l\_GDP$

	Coefficient	Std. Error	t-ratio	p-value	
const	-15.1786	1.63779	-9.2677	<0.00001	***
$l\_K$	0.66869	0.212248	3.1505	0.01173	**
$l\_L$	1.55067	0.532088	2.9143	0.01719	**
Mean dependent var	13.85807		S.D. dependent var	0.155176	
Sum squared resid	0.006618		S.E. of regression	0.027117	
R-squared	0.975014		Adjusted R-squared	0.969462	
F(2, 9)	175.6025		P-value(F)	6.16e-08	
Log-likelihood	27.98983		Akaike criterion	-49.97965	
Schwarz criterion	-48.52493		Hannan-Quinn	-50.51824	
rho	0.280857		Durbin-Watson	0.979910	
White's test for heteroskedasticity -					
Null hypothesis: heteroskedasticity not present					
Test statistic: LM = 10.5425					
with p-value = $P(\text{Chi-square}(5) > 10.5425) = 0.0612439$					
LM test for autocorrelation up to order 1 -					
Null hypothesis: no autocorrelation					
Test statistic: LMF = 0.932914					
with p-value = $P(F(1,8) > 0.932914) = 0.362393$					
RESET test for specification -					
Null hypothesis: specification is adequate					
Test statistic: $F(2, 7) = 10.6811$					
with p-value = $P(F(2, 7) > 10.6811) = 0.00746883$					
Test for normality of residual -					
Null hypothesis: error is normally distributed					
Test statistic: $\text{Chi-square}(2) = 1.63745$					
with p-value = 0.440994					

**Table 2.** Estimation and diagnostic of the OLS model. Dependent variable:  $l\_GDPc$

	Coefficient	Std. Error	t-ratio	p-value	
$l\_Kc$	0.323928	0.0664947	4.8715	0.00065	***
$l\_Lc$	0.831137	0.173851	4.7808	0.00074	***
Mean dependent var	11.14063		S.D. dependent var	0.223449	
Sum squared resid	0.021566		S.E. of regression	0.046439	
R-squared	0.999986		Adjusted R-squared	0.999984	
F(2, 10)	345428.9		P-value(F)	6.35e-25	
Log-likelihood	20.90205		Akaike criterion	-37.80410	
Schwarz criterion	-36.83428		Hannan-Quinn	-38.16316	
rho	0.503041		Durbin-Watson	0.985198	
White's test for heteroskedasticity -					
Null hypothesis: heteroskedasticity not present					
Test statistic: LM = 3.30193					
with p-value = $P(\text{Chi-square}(5) > 3.30193) = 0.653546$					
LM test for autocorrelation up to order 1 -					
Null hypothesis: no autocorrelation					
Test statistic: LMF = 2.74639					
with p-value = $P(F(1,9) > 2.74639) = 0.131853$					
RESET test for specification -					
Null hypothesis: specification is adequate					
Test statistic: $F(2, 8) = 0.416865$					
with p-value = $P(F(2, 8) > 0.416865) = 0.672641$					
Test for normality of residual -					
Null hypothesis: error is normally distributed					
Test statistic: $\text{Chi-square}(2) = 0.521285$					
with p-value = 0.770556					

**Table 3.** Estimation and diagnostic of the OLS model. Dependent variable: l\_GDP

	Coefficient	Std. Error	t-ratio	p-value	
time	0.0240464	0.00178949	13.4376	<0.00001	***
l_L	1.44282	0.00122147	1181.2151	<0.00001	***
Mean dependent var	13.85807		S.D. dependent var	0.155176	
Sum squared resid	0.004513		S.E. of regression	0.021244	
R-squared	0.999998		Adjusted R-squared	0.999998	
F(2, 10)	2553474		P-value(F)	2.88e-29	
Log-likelihood	30.28681		Akaike criterion	-56.57362	
Schwarz criterion	-55.60380		Hannan-Quinn	-56.93268	
rho	0.339576		Durbin-Watson	0.919227	
White's test for heteroskedasticity - Null hypothesis: heteroskedasticity not present Test statistic: LM = 9.67768 with p-value = P(Chi-square(5) > 9.67768) = 0.0849004			LM test for autocorrelation up to order 1 - Null hypothesis: no autocorrelation Test statistic: LMF = 1.05082 with p-value = P(F(1,9) > 1.05082) = 0.332081		
Test for normality of residual - Null hypothesis: error is normally distributed Test statistic: Chi-square(2) = 0.85072 with p-value = 0.653535			RESET test for specification - Null hypothesis: specification is adequate Test statistic: F(2, 8) = 25.1876 with p-value = P(F(2, 8) > 25.1876) = 0.000352732		

**Table 4.** Estimation and diagnostic of the OLS model. Dependent variable: l\_GDPc

	Coefficient	Std. Error	t-ratio	p-value	
const	5.20913	0.654879	7.9543	0.00002	***
l_Lc	0.872295	0.101666	8.5800	0.00001	***
time	0.0255877	0.00452404	5.6559	0.00031	***
Mean dependent var	11.14063		S.D. dependent var	0.223449	
Sum squared resid	0.008883		S.E. of regression	0.031417	
R-squared	0.983826		Adjusted R-squared	0.980231	
F(2, 9)	273.7195		P-value(F)	8.70e-09	
Log-likelihood	26.22367		Akaike criterion	-46.44734	
Schwarz criterion	-44.99262		Hannan-Quinn	-46.98593	
rho	0.191649		Durbin-Watson	1.581690	
White's test for heteroskedasticity - Null hypothesis: heteroskedasticity not present Test statistic: LM = 5.95649 with p-value = P(Chi-square(5) > 5.95649) = 0.310476			LM test for autocorrelation up to order 1 - Null hypothesis: no autocorrelation Test statistic: LMF = 0.304651 with p-value = P(F(1,8) > 0.304651) = 0.596059		
Test for normality of residual - Null hypothesis: error is normally distributed Test statistic: Chi-square(2) = 0.609357 with p-value = 0.73736			RESET test for specification - Null hypothesis: specification is adequate Test statistic: F(2, 7) = 0.204028 with p-value = P(F(2, 7) > 0.204028) = 0.820122		

**Table 5.** Estimation and diagnostic of the OLS model. Dependent variable: gGDP

	Coefficient	Std. Error	t-ratio	p-value	
const	0.0316081	0.00666837	4.7400	0.00106	***
gL	0.875713	0.343222	2.5515	0.03112	**
Mean dependent var	0.040261		S.D. dependent var	0.023715	
Sum squared resid	0.003264		S.E. of regression	0.019042	
R-squared	0.419726		Adjusted R-squared	0.355251	
F(1, 9)	6.509903		P-value(F)	0.031121	
Log-likelihood	29.06734		Akaike criterion	-54.13469	
Schwarz criterion	-53.33890		Hannan-Quinn	-54.63632	
rho	0.077425		Durbin-Watson	1.705988	
White's test for heteroskedasticity - Null hypothesis: heteroskedasticity not present Test statistic: LM = 0.14083 with p-value = P(Chi-square(2) > 0.14083) = 0.932007			LM test for autocorrelation up to order 1 - Null hypothesis: no autocorrelation Test statistic: LMF = 0.0594553 with p-value = P(F(1,8) > 0.0594553) = 0.813496		
Test for normality of residual - Null hypothesis: error is normally distributed Test statistic: Chi-square(2) = 4.08096 with p-value = 0.129966			RESET test for specification - Null hypothesis: specification is adequate Test statistic: F(2, 7) = 1.18041 with p-value = P(F(2, 7) > 1.18041) = 0.361614		

**Table 6.** Estimation and diagnostic of the OLS model. Dependent variable: gGDPc

	Coefficient	Std. Error	t-ratio	p-value	
const	0.0282374	0.0122829	2.2989	0.04708	**
gLc	0.744785	0.150376	4.9528	0.00079	***
Mean dependent var	0.042815		S.D. dependent var	0.072423	
Sum squared resid	0.014079		S.E. of regression	0.039551	
R-squared	0.731588		Adjusted R-squared	0.701764	
F(1, 9)	24.53054		P-value(F)	0.000788	
Log-likelihood	21.02717		Akaike criterion	-38.05434	
Schwarz criterion	-37.25855		Hannan-Quinn	-38.55597	
rho	-0.186312		Durbin-Watson	2.341102	
White's test for heteroskedasticity - Null hypothesis: heteroskedasticity not present Test statistic: LM = 0.0388568 with p-value = P(Chi-square(2) > 0.0388568) = 0.980759			LM test for autocorrelation up to order 1 - Null hypothesis: no autocorrelation Test statistic: LMF = 0.30038 with p-value = P(F(1,8) > 0.30038) = 0.5986		
Test for normality of residual - Null hypothesis: error is normally distributed Test statistic: Chi-square(2) = 1.42324 with p-value = 0.490848			RESET test for specification - Null hypothesis: specification is adequate Test statistic: F(2, 7) = 0.652857 with p-value = P(F(2, 7) > 0.652857) = 0.549571		

**Table 7.** Estimation and diagnostic of the OLS model. Dependent variable: l\_GDP

	Coefficient	Std. Error	t-ratio	p-value	
const	-596.904	122.311	-4.8802	0.00122	***
l_K	99.2252	20.7219	4.7884	0.00138	***
l_L	-97.4567	20.8184	-4.6813	0.00158	***
sq_l_KL	-4.14363	0.871202	-4.7562	0.00143	***
Mean dependent var	13.85807		S.D. dependent var	0.155176	
Sum squared resid	0.001729		S.E. of regression	0.014701	
R-squared	0.993472		Adjusted R-squared	0.991025	
F(3, 8)	405.8541		P-value(F)	4.46e-09	
Log-likelihood	36.04342		Akaike criterion	-64.08683	
Schwarz criterion	-62.14721		Hannan-Quinn	-64.80495	
rho	-0.289578		Durbin-Watson	2.557439	
White's test for heteroskedasticity -			LM test for autocorrelation up to order 1 -		
Null hypothesis: heteroskedasticity not present			Null hypothesis: no autocorrelation		
Test statistic: LM = 9.35511			Test statistic: LMF = 0.746575		
with p-value = P(Chi-square(8) > 9.35511) = 0.31323			with p-value = P(F(1,7) > 0.746575) = 0.416185		
Test for normality of residual -			RESET test for specification -		
Null hypothesis: error is normally distributed			Null hypothesis: specification is adequate		
Test statistic: Chi-square(2) = 2.92143			Test statistic: F(2, 6) = 0.937102		
with p-value = 0.23207			with p-value = P(F(2, 6) > 0.937102) = 0.442419		

**Table 8.** Estimation and diagnostic of the OLS model. Dependent variable: l\_GDPc

	Coefficient	Std. Error	t-ratio	p-value	
const	1.34905	0.667262	2.0218	0.07391	*
l_Lc	1.14609	0.111077	10.3179	<0.00001	***
sq_l_KLc	0.0189924	0.00641013	2.9629	0.01589	**
Mean dependent var	11.14063		S.D. dependent var	0.223449	
Sum squared resid	0.020481		S.E. of regression	0.047704	
R-squared	0.962709		Adjusted R-squared	0.954422	
F(2, 9)	116.1731		P-value(F)	3.73e-07	
Log-likelihood	21.21172		Akaike criterion	-36.42344	
Schwarz criterion	-34.96872		Hannan-Quinn	-36.96203	
rho	0.453088		Durbin-Watson	1.084647	
White's test for heteroskedasticity -			LM test for autocorrelation up to order 1 -		
Null hypothesis: heteroskedasticity not present			Null hypothesis: no autocorrelation		
Test statistic: LM = 3.00996			Test statistic: LMF = 2.02611		
with p-value = P(Chi-square(5) > 3.00996) = 0.69845			with p-value = P(F(1,8) > 2.02611) = 0.192423		
Test for normality of residual -			RESET test for specification -		
Null hypothesis: error is normally distributed			Null hypothesis: specification is adequate		
Test statistic: Chi-square(2) = 1.69812			Test statistic: F(2, 7) = 0.184855		
with p-value = 0.427817			with p-value = P(F(2, 7) > 0.184855) = 0.835154		

**Table 9.** Estimation the NLS model.  $\ln GDP = \ln(\gamma) - (\mu/\rho)\ln(\delta * K1^{(-\rho)} + (1-\delta) * L1^{(-\rho)})$

	Estimate	Std. Error	t-ratio	p-value	
gamma	2.2245	0.337129	6.5983	0.00010	***
mu	2.2245	0.337129	6.5983	0.00010	***
rho	-0.0191591	0.0524633	-0.3652	0.72340	
delta	0.253279	0.0581017	4.3592	0.00183	***
Mean dependent var	13.85807		S.D. dependent var	0.155176	
Sum squared resid	0.006629		S.E. of regression	0.027140	
R-squared	0.974973		Adjusted R-squared	0.969412	
Log-likelihood	27.98000		Akaike criterion	-49.96000	
Schwarz criterion	-48.50528		Hannan-Quinn	-50.49859	
rho	0.276942		Durbin-Watson	0.984424	

**Table 10.** Estimation the NLS model.  $\ln GDPc = \ln(\gamma) - (\mu/\rho)\ln(\delta * Kc^{(-\rho)} + (1-\delta) * Lc^{(-\rho)})$

	Estimate	Std. Error	t-ratio	p-value	
gamma	1.14683	0.110959	10.3356	<0.00001	***
mu	1.14683	0.110959	10.3356	<0.00001	***
rho	-0.0697593	0.0844433	-0.8261	0.43010	
delta	0.205863	0.112897	1.8235	0.10154	
Mean dependent var	11.14063		S.D. dependent var	0.223449	
Sum squared resid	0.020508		S.E. of regression	0.047735	
R-squared	0.962661		Adjusted R-squared	0.954363	
Log-likelihood	21.20395		Akaike criterion	-36.40789	
Schwarz criterion	-34.95317		Hannan-Quinn	-36.94648	
rho	0.452835		Durbin-Watson	1.084488	

**Received:** 11 February 2015 • **Accepted:** 19 February 2015

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